

# Long-Term Investment

## Asset-Class Based Capital Budgeting

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# Apologies

- As **Research Affiliates**' audience, you are probably more interested in investments than corporate finance.
  - The area of **Corporate finance** is typically about longer-term (and difficult to reverse) decisions
  - The area of **Investments** is about investments that allow quick entry and exit.
- But indulge me—some of this will be relevant for investors and asset managers, too.

# What is the most important topic in Corporate Finance?

## Capital Budgeting

- Choosing good projects is the most value-important and ubiquitous question.
- It's our Bread and Butter
  - Corporate Governance? Capital Structure?
- Let's make sure we get capital budgeting right!

# IRR and NPV Logic

- Should you invest their money on behalf of your investors, or should you instead return it?
- Should you demand higher average returns for projects for which similar/equivalent projects are expected to deliver higher returns elsewhere?
- What if the most common models' claims about these other opportunities are wrong?

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# What do we **really** know about Equity Returns?

- Lots of caveats on CAPM/FFM in Fama-French:1997 ...but we still use the models.
- Most academic evidence is based on predictions of 1-mo ( $\ll$ 1 year) ahead stock returns.
  - CAPM fails even on 1-month ahead prediction.
  - Sadly, even FFM may or may not work.
  - (Momentum and book-to-market may work—this is not the FFM!)

Do any corporations really care about the cost of capital for 1-mo (or 1-yr) projects?

- Interesting projects last 5 years to 100 years

# So what do we know about the Eq Prem?

- We **believe** debt to be cheaper than equity.

(Need not be risk-aversion. Tax benefits, liquidity, sentiment, asset-class segmentation, industry segmentation, etc., could induce the same differential as risk aversion and differential systematic risk exposure.)

- ...but let's look at this one skeptically, too.

# What can we do to help?

- Half of you won't believe **any** evidence, and not abandon the models because you believe they can be useful:
  - (1) Let me show you a few more coffin nails:
    - (1a) If the models held, how should you use them?
    - (1b) Show evidence how badly they fail long-term.
- The other half will tell me it was obvious.

(If you are finance profs, you will go back and teach only the CAPM/FFM, anyway.)

  - (2) What could and should you use instead?

Fama-French:1997 takeaways: first group remember that applications should use industries instead of firms. second subgroup remember that small variations in assumptions come up with completely different estimates.



# Surprising and Not Surprising

So here is what I will “sell” you:

- Some of what I will say will seem obviously true.
- Some of it you will know.
- Some of it will just be repackaged truth—but remember that the Church repeats the gospel many times, too.
- Some of it will be surprising.

# Equity Premium

- What was the extra rate of return that a tax-exempt investor would have earned on stocks over long-term Treasuries, from 1970 to last year?

< 1%/year

- not poor stock returns, but higher long-term bond yields.
- the oft-quoted 6-8% are arithmetic returns from 1926 to 1970 vis-a-vis Treasury bills. R u kidding?
- do not expect high equity premia, based on past equity returns. wrong and irrelevant.

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# Quick Summary of Presentation Figs

We test reasonable model implementation and use; we do not test the model per se:

- Only 49 Industries. (Indiv. firms = worse. no IPOs, survival)
- 1962–2010. (21,683 stocks / 2.1m firm-months)
- Vasicek betas, daily data, 5 year windows. FFM=MV.
- 30-50 year prevailing premia estimates.
- Use models to calculate expected rates of return.
- How do model  $X$ ="expected rates of return" *predict* future  $Y=E(r)$  or future actual  $Y=r$ ? Ideally,  $\hat{\gamma}_1 = 1$ . Useful model if  $\hat{\gamma}_1 > 0$ .
- Xsect Q: Always out-of-sample, Fama-Macbeth like.
- All standard errors are from **placebo**: randomize returns across firms/industries on same date. Keeps irregular data matrix intact. We do not randomize factor premia—if we destroyed them, NULL would look even better.

Sort of a best-use-case scenario

Presentation omits MANY robustness checks.

## Let's Rock

(Easier to show than to explain. Equities Only! Not Unlevered!)

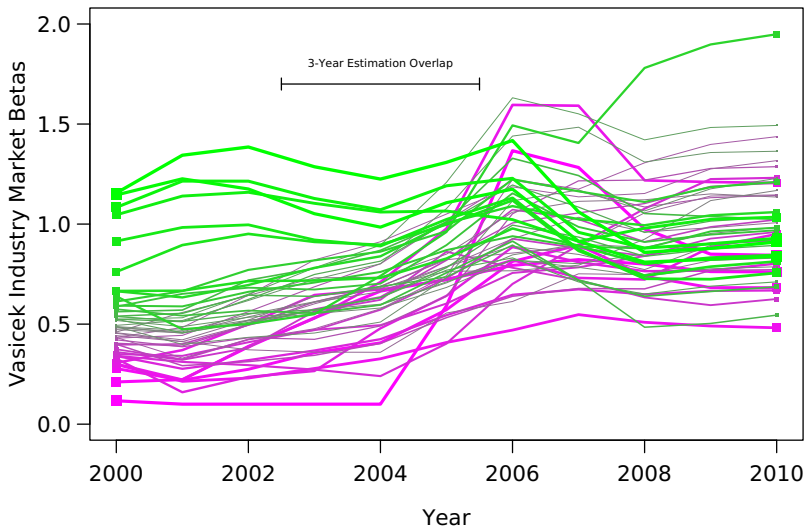
# Point #1 a:

Even if you are a believer, your models' estimates/loadings do not have much long-term stability. (Stability is necessary, but not sufficient. Stability is *not* a tough model criterion. Needed in long-term applications.)

I will show you that today's beta estimates cannot be used for cash flows in 5-10 years.

- This is *after* Bayesian Vasicek exposure shrinking.
- CAPM estimates, say, 5% E(R) difference in cc today
  - ⇒ optimally use= 2% E(R) diff for 5-year's CFs (Car)
  - ⇒ optimally use= 1% E(R) diff for 20-year's CFs (Building)
  - ⇒ optimally use= 0% E(R) diff for 50-year's CFs (Land)
- Is this a good use of your research money? (Gaming?)

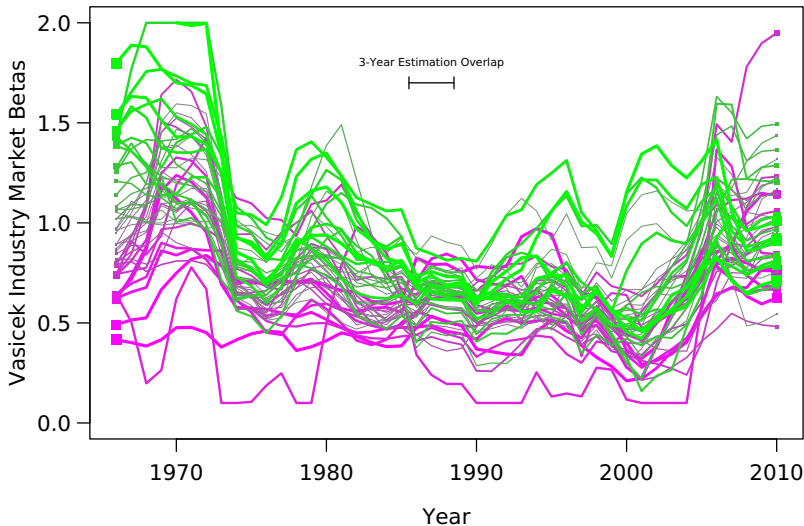
# Beta Stability of Equity



(10-year autocorrelation for 49 industries is about 0.4.)

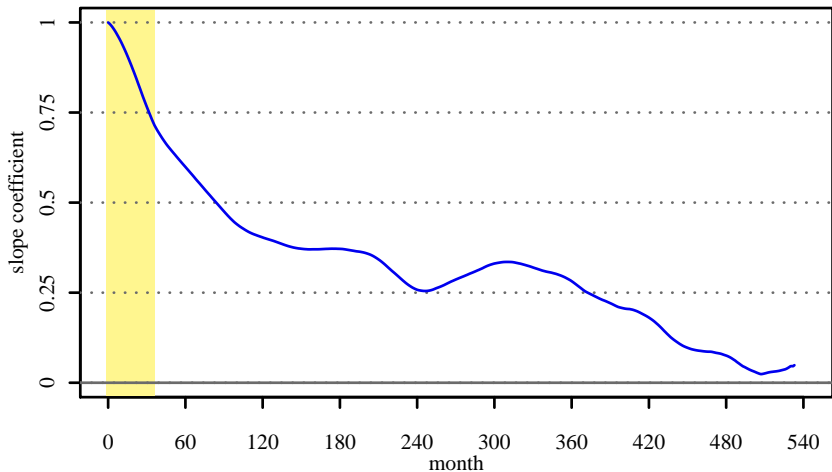


# Beta Stability



(50-year autocoeff for 49 industries is about 0.)  
(FFM loadings are similarly or more unstable.)

# X-Sectional Correlation of Industry ER over Time



Warning: final data points are based on very few regressions.

# Optimal Weight on Vasicek

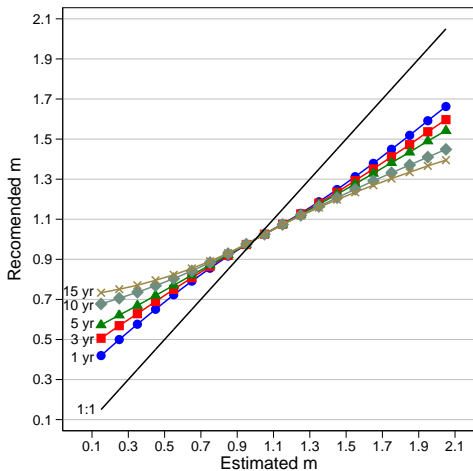
- Assume CAPM is true. Simulate World (know true ER).
  - Match beta reversion:  $m_t \approx 0.01 \times 1 + 0.99 \times m_{t-1} + e$
  - Match  $E(M)$ ,  $sd(M)$ ,  $sd(e)$ .  $sd[E(R)]$ .
  - No LR industry own means. just long-run but temp moves.
- Estimate Vasicek beta and cost of capital.
- Find best  $\theta$  weighted Vasicek beta /  $E(r)$  and “1.1” that minimizes MSE difference to true  $E(r)$ .

Double shrinkage:

- Shrinkage / Vasicek says put some weight on 1.1, some weight on your own beta.
- With autocorr of beta, we need to shrink more.

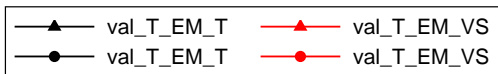
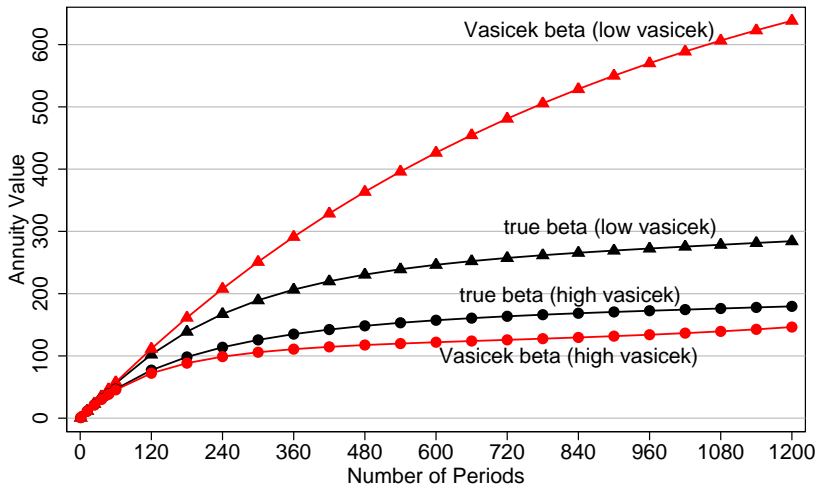
# How should you double-shrink Beta?

What shrinkage tells you, vs what you should be using:



X-axis is already shrunk!

# Annuities Value Effects



# Point #1b:

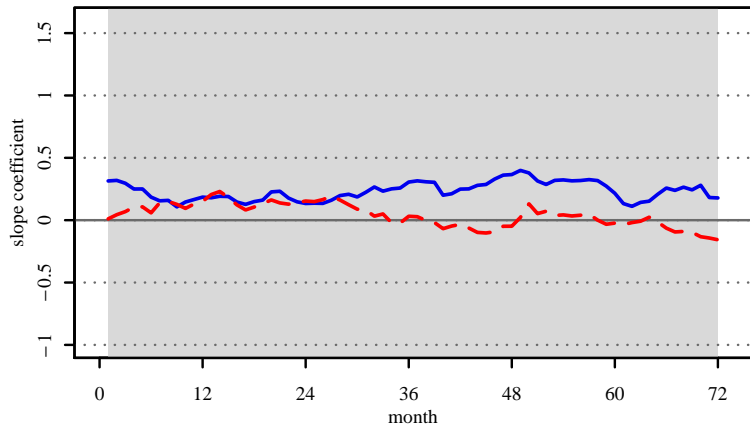
- Preceding was internal model validity. It did not look at actual “other project” opportunity costs—actual rates of return delivered.
- So, did the models have any predictive ex-ante power for what other projects with similar model riskiness actually delivered ex-post?
- Q: You know the 1-mo evidence. What do you think the 10-yr evidence is?

Predict future actual returns with your model returns (not with model ingredient factors).

$$r_i = \gamma_0 + \gamma_1 \times E(R_i) + \text{noise}$$

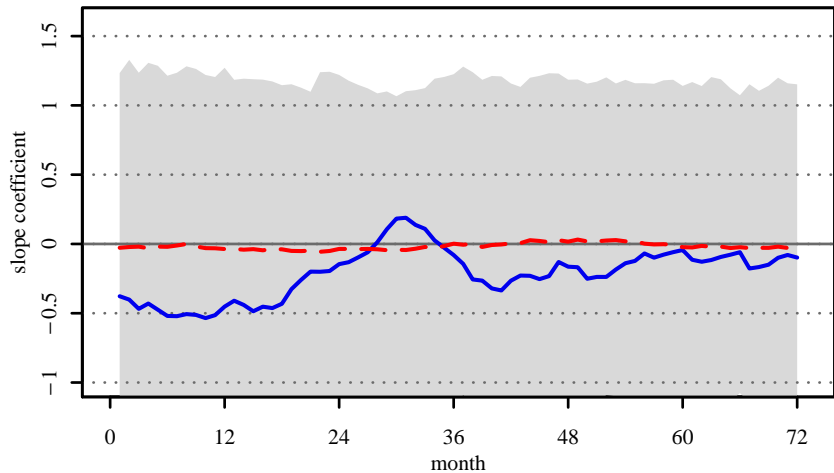
Aggregate over time. Doesn't matter much.

# CAPM – Marginal Returns



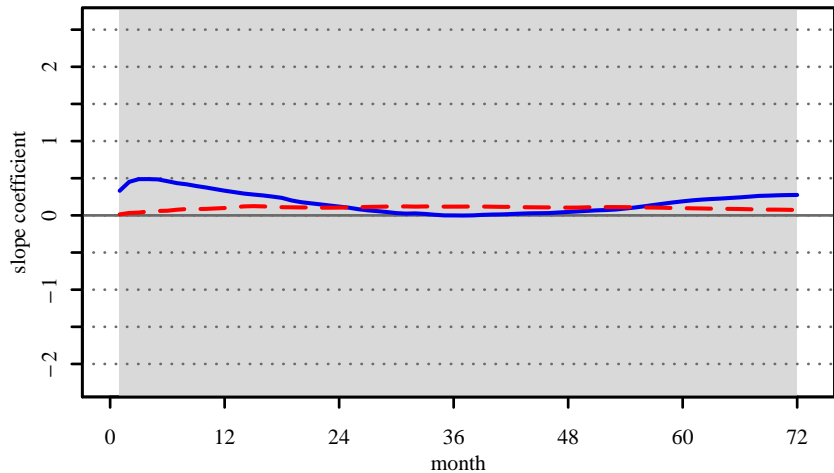
IAW: Stop and Explain Graph.

# FFM – Marginal Returns

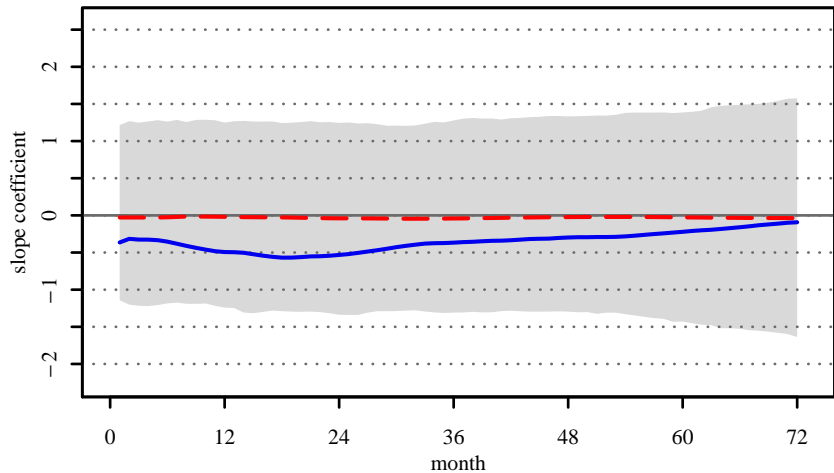




# CAPM – Compound Returns



# FFM – Compound Returns



# Does the FFM hold??

- Sorry, no. Not even over short intervals.
- Some factors inside it have worked: B-M and Momentum.
- Recent papers suggest only about 600 different factors that have worked...in-sample. After publication, about 51% work, the other 49% fail.
- Knowledge of poor out-of-sample predictive ability on ER can be very useful in forming intelligent portfolios.  
e.g., tilt towards low-beta. investigate crash vs. non-crash behavior. use existing fin'l markets instruments to hedge against your model ignorance.

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Did highly levered firms offer higher average returns?  
Sadly no

## Financial Genius



# Conclusions?!

Neither the FFM nor the CAPM model had actual-return forecasting power over long-horizons, either. Not even a close call.

As benchmark providers for what expected returns projects should have provided over the long term, both models have utterly failed “use test” in the past. Not even a close call.

...yet 70% of firms continue that this is what your projects have to meet?!?

...was not a model test, but a test of our ability to properly use models. Thus, no EIV (measure!=proxy).

Confess: Were your priors that the models gave you good estimates or lousy estimates??

# Now What?

It takes a model to beat a model.

What should we teach?



# Asset-Based Capital Budgeting

- We are interested in asset betas, not equity betas:  
 $E(R_A) = w_E \times E(R_E) + w_D \times E(R_D)$ .
- For whatever reason (imperfect markets?), all equities seem to offer similar long-term average returns.
- If your  $E(R_D) < E(R_E)$ , **and** you can predict own future D/E, then you can predict future **asset** cost-of-capital.
- Leverage ratios are often predictable and/or stable.
- It's a standard CorpFin (not AssPrc) approach. Assign one cost of capital to equity. Assign one cost of capital to debt. (Debt capacity can be useful.) Take wght avg.
- Corporate income tax deduction may well be most of the reason why bonds end up being cheaper corporate financing than stocks.

## Asset-Based Capital Budgeting

For long-term standard corporate projects:

- Assume  $\beta \approx 1$ .
- Use (tax-adj) cost of debt capital, often promised  $\approx$  expected
- Assess your planned/intended project debt-ratio.
- (Possibly worry about cost of capital of NFL.)  
 $\Rightarrow E(R_A) = \hat{w}_E \times (6-8\%) + (1 - \hat{w}_E) \times E(R_D) \times (1 - \tau)$

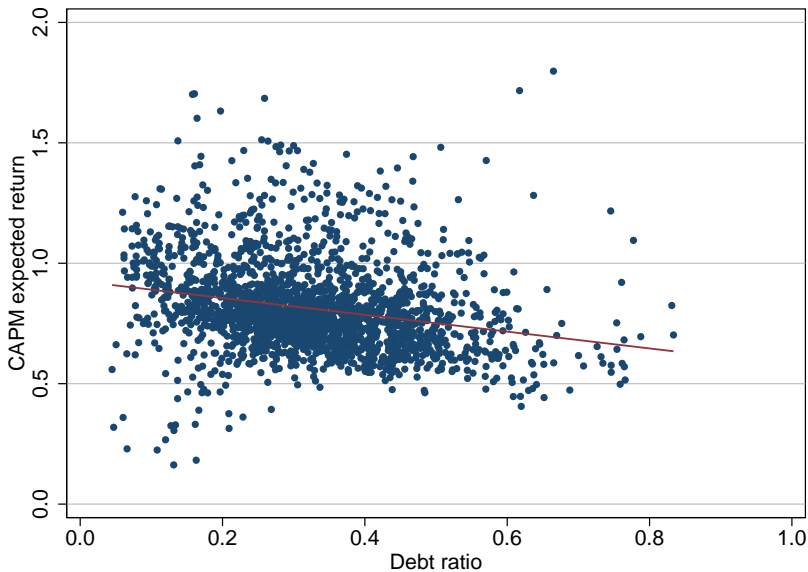
Spend your time worrying about  $E(CF)$  instead.

# Mistakes?

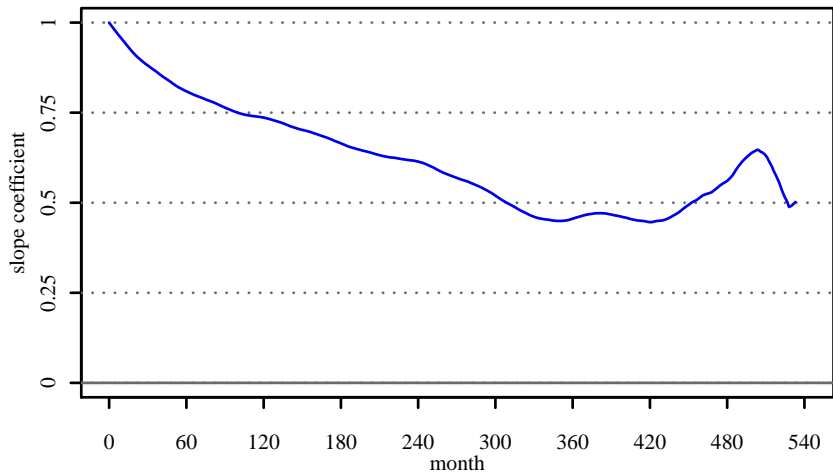
How bad are ABC errors relative to true CAPM/FFM?

- Don't use this model for (short-term) bond pricing or for 99% levered companies. Use this model for normal firms/projects.
- Leverage ameliorates further asset-beta errors. Errors in  $E(R_E)$  typically map into lower  $E(R_A)$  errors. High leverage, high  $E(R_E)$  errors are mult. by  $1 - w_D$ .
  - High-leverage same-asset-beta firms should have had high  $w_E$ ,  $E(R_E)$ , and  $E(R_D)$ .
  - Empirical Evidence:  
high LR = high  $E(R_E)$ ? see next pg.  
high LR = high  $E(R_D)$ ? maybe. see Altman etc.

# Leverage Ratios and Model Equity Expected Rates



# Leverage Ratios and Future Leverage Ratios



(but debt may well be your decision variable, so you don't need this)

# Is Corporate Debt Really Cheaper?

We think so, but even this is **not** 100% clear.

Ibbotson (2010), Table 2.1, geometric:

- Large Company Stocks: 9.8% (sd=20%)
- LT Corp bonds: 5.9% (10%)

Is the (pre-tax) corporate cost of bonds really lower? 4% difference is not statistically significant. But after-tax cost of (short-term) bonds does seem meaningfully lower.

Fortunately, like  $w_D$ , this can be a firm-specific CFO judgment call. (From the inside, in an imperfect market, quoted yields may even be your expected cost of debt.)

# Natural Consequences

Optimal behavior is similar to some imperfect-market corporate theories, but ABC is more pragmatic and less specialized.

- Value debt-financed projects (like buildings) more highly than equity-financed projects (like R&D).
- Don't put equity money into cash. The presumed reduction in equity betas which reduces the cost of capital is *not* there. Holding cash is not worth it.
- Take projects until the marginal cost of debt is equal to the marginal cost of equity and the marginal return on projects.
- Conjecture—firm may incur sudden sharp increase in the cost of debt and equity when “overlevered.”

# Advantages

- Most Important: (Academic) Integrity.
- Truth in Advertising.
- Not priors=faitth-based capital budgeting.
- Lots of tough problems become much easier.
  - E.g., real options turn from real hard into real simple problems.
  - E.g., tax shelters are simple now. APV and WACC yield the same results.
  - E.g., behavioral finance may be easier to understand.
- Less distraction with unimportant details.
- No claims to short-term AP. ABC is not all the answers.



# Managerial Advantages

- Focus more on time and less on risk adjustments.
- Focus more on expected cash flows—which is where the focus should be!
- Focus more on failure probabilities (cash flows).
  - Higher expected rates of return for high-failure projects based on an asset-pricing model is the wrong crutch.
  - Maybe helped by a volatility-based  $E(R)$  model?
- Easier (=cheaper) to use same cost of equity capital for all projects.
- Less gaming.

## Unhelpful Appendix

# (1) Model for #1A: Dynamic-Beta CAPM

$$m_{i,t}^{true} \stackrel{iid}{\sim} N(\mu_m, \sigma_m) \quad t = -35 \quad m_{i,t}^{true} = \mu_{dm} + \rho_{dm} m_{i,t-1}^{true} + \varepsilon_{dm} t = -34, \dots, 180 \quad (1)$$

$$\varepsilon_{dm} \stackrel{iid}{\sim} N(0, \sigma_{dm}^2) \quad M_t \stackrel{iid}{\sim} N(\mu_M, \sigma_M^2) t = -599, \dots, 0 \quad (2)$$

$$MP \sim N(\mu_M, \sigma_{MP}^2) \quad (3)$$

$$r_{i,t} = r_f + m_{i,t}^{true} M_t + \varepsilon_{i,t} \quad t = -35, \dots, 0 \quad \varepsilon_i \stackrel{iid}{\sim} N(0, \sigma_\varepsilon^2) \quad (4)$$

$$E(r_{i,t})^{true} = r_f + m_{i,t}^{true} \mu_M \quad t = 0, 1, \dots, 180 \quad (5)$$

Manager estimates her loading over 36 periods.

$$r_{i,t} - r_f = \alpha_i + m_i^{est} M_t \quad -35 \leq t \leq 0 \quad (6)$$

Manager chooses her cost of capital by weighting her own estimated cost of capital and the cross sectional mean,

$$COND = E(r_i)^{est} = r_f + m_i^{est} MP \quad (7)$$

$$UNCO = r_f + \mu_M MP \quad (8)$$

We find the optimal weight by simulating the model and solving

$$\min_{w_t} E \left[ \left( w_t UNCO + (1 - w_t) COND - E(r_{i,t})^{true} \right)^2 \right] \quad t = 0, \dots, 180 \quad (9)$$

Note that the dynamics of  $m_{i,t}$  in equation 1 can be represented as

$$m_{i,t}^{true} = \theta K + (1 - \theta) m_{i,t-1}^{true} + \varepsilon_{dm} \quad (10)$$

with  $\theta = 1 - \rho_{dm}$ ,  $K = \frac{\mu_{dm}}{1 - \rho_{dm}}$ .

# Estimation

**Direct estimation** We set  $\mu_m, \sigma_m, \sigma_E, \mu_M, \sigma_M$  and  $r_f$  equal to the corresponding population moments. See table pop dynamics.

**Calibration** We set  $\mu_{dm}, \rho_{dm}$  and  $\sigma_{dm}$  to fit the population moments in tables 49 ind. The calibration process for the 49 industries simulations is as follows:

- We construct a panel, size 49 industries and 108 periods ( $t = -35, \dots, 72$ ), of true market loadings. We draw  $t = -35$  loadings for the 49 industries from a normal distribution with mean  $\mu_m$  and std  $\sigma_m$  (see table ??). True loadings evolve over the additional 107 periods according to equation 1.
- We draw a ts of factor (M) realizations from a normal distribution with mean  $\mu_M$  and variance  $\sigma_M$ . (See table ??.)
- We construct a panel of realized returns using the ts of factor realizations, the panel of true loadings and  $\sigma_E$  from table ??.
- We construct a panel **estimated** loadings using the realized returns and the factor realizations.
- We construct find expected returns using the estimated loadings and market premium drawn from a normal distribution with mean  $\mu_M$  and variance  $\sigma_{MP}$ .
- We repeat this process 1000 times and present the means of the collected moments in table tables ??.

# Dynamic model parametrization, CAPM, direct estimation

model parameter	sample	value	source
$\mu_M$		0.458	XMKT 600 month ending at 2010/12
$\sigma_M$		4.525	XMKT 600 month ending at 2010/12
$\sigma_{MP}$		0.185	standard error of $\mu_M$
$rf$		0.049	rf 36 month ending at 2010/12
$\sigma_E$	49 industries	4.797	average of error term std in loading estimation r
$\mu_m$	49 industries	1.115	mean XMKT loading
$\sigma_m$	49 industries	0.309	std XMKT loading
$\sigma_E$	all CRSP	13.030	average of error term std in loading estimation r
$\mu_m$	all CRSP	1.097	mean XMKT loading
$\sigma_m$	all CRSP	0.779	std XMKT loading

# Dynamic model parametrization, matched moments, 49 industries

statistic	49 industries sample		calibration results*		
	value	s.e.	$t = 0$	$t = 36$	$t = 72$
$\mu_m$	1.115	0.009	1.113	1.113	1.111
$\sigma_m$	0.309	0.004	0.343	0.340	0.340
$corr(m_t, m_{t+1})$	0.987	0.001	0.992		
$corr(m_t, m_{t+36})$	0.560	0.008	0.577		
$corr(m_t, m_{t+72})$	0.444	0.009	0.423		
$std(E(ret)^{est})$	0.188	0.003	0.158	0.158	0.156

\* Chosen calibrated parameters are  $\mu_{dm} = 0.01$ ,  $\rho_{dm} = 0.991$ ,  $\sigma_{dm} = 0.04$ .

Population moments are ts averages of the monthly data 1966/07 to 2010/12.

Population market loadings were estimated using 36 historical month

Population expected returns were constructed using constant risk free rate (0.049) and 600 months running average of XMKT.

# CRSP, betas below 0.5 at $t=0$ , moments in population vs simulations

statistic	All CRSP sample			calibration results*		
	t=0	t=36	t=72	t=0	t=36	t=72
$\mu_m$	0.173	0.657	0.680	0.006	0.585	0.754
$s.e.(\mu_m)$	0.005	0.008	0.008	0.003	0.004	0.003
$\sigma_m$	0.325	0.623	0.620	0.409	0.678	0.670
$s.e.(\sigma_m)$	0.007	0.008	0.008	0.002	0.005	0.004
$std(E(ret)^{est})$	0.222	0.403	0.387	0.196	0.306	0.296
$s.e.(std(E(ret)^{est}))$	0.005	0.006	0.005	0.008	0.012	0.014
$corr(m_t, m_{t+1})$	0.924			0.965		
$corr(m_t, m_{t+36})$	-0.003			0.288		
$corr(m_t, m_{t+72})$	0.021			0.192		

# CRSP, betas above 1.5 at t=0 , moments in population vs simulations

statistic	All CRSP sample			calibration results*		
	t=0	t=36	t=72	t=0	t=36	t=72
$\mu_m$	2.112	1.477	1.357	2.045	1.537	1.389
$s.e.(\mu_m)$	0.010	0.012	0.012	0.003	0.003	0.002
$\sigma_m$	0.591	0.789	0.793	0.440	0.680	0.673
$s.e.(\sigma_m)$	0.009	0.012	0.012	0.002	0.005	0.004
$std(E(ret)^{est})$	0.387	0.510	0.498	0.211	0.307	0.298
$s.e.(std(E(ret)^{est}))$	0.006	0.007	0.007	0.008	0.012	0.014
$corr(m_t, m_{t+1})$	0.950			0.969		
$corr(m_t, m_{t+36})$	0.152			0.306		
$corr(m_t, m_{t+72})$	0.122			0.206		



## (2) List of Omitted Variations

- Firms rather than Industries. We do not have project data. Firms with IPOs. (Problem: Survival.)
- Variations in factor premia assessments. Full-sample ex-post. 50-year. 30-year.
- No-adjustment beta. Blume-adjustment. ML adjustment. Dimson beta. Conditional Vasicek beta (size, leverage, book-market).
- Beta = 5 years, daily. 5-years monthly (worse). excess vs. raw regressions.
- Equal-weighted vs. value-weighted factor portfolios
- Industry portfolios, equal-weighted vs value-weighted. 49 vs. more.
- Forecast compound returns with and without volatility adjustment. (1/2 sigma-squared)
- Forecast discount factors.
- Model expected return calculation:

$$E_t[r_i] = r_{f,t} + \hat{\beta}_{i,M} \cdot \overline{XMK}_t,$$

$$E_t[r_i] = r_{f,t} + \hat{\beta}_{i,M} \cdot \overline{XMK}_t + \hat{\beta}_{i,S} \cdot \overline{SMB}_t + \hat{\beta}_{i,H} \cdot \overline{HML}_t.$$

- Placebo-adjustment for overlap. Non-overlap. Omitted Model Factors.
- Worry about worry—placebo seems most robust.
- HML model, instead of FFM model.